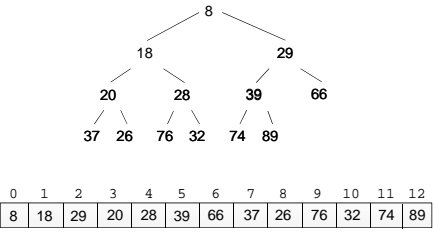


CSIS 3103
Ch 6: Priority Queues

Implementing a Heap

- A complete binary tree can be implemented efficiently using an array
- First element stores a reference to the root data

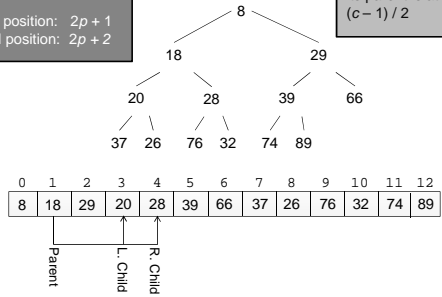


Implementing a Heap

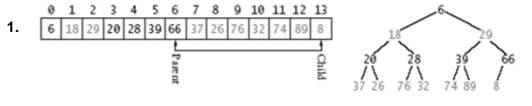

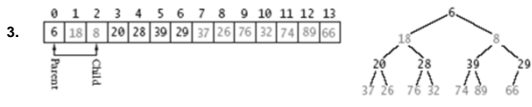
For a node at position p ,

L. child position: $2p + 1$
R. child position: $2p + 2$

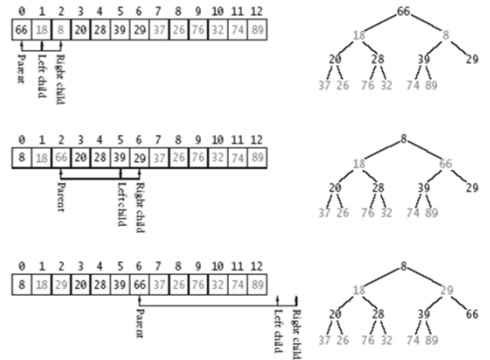
For node at position c
its parent is at $(c - 1) / 2$



Inserting into a Heap

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- 
- 

Deleting from a Heap



Priority Queues

- Another kind of waiting line but not FIFO like a queue
- In a *priority queue*, only the highest-priority item is accessible
- A heap is used to implement a priority queue

Insertion into a Priority Queue

Insertion into a Priority Queue

pages = 1
title = "web page 1"

pages = 4
title = "history paper"

After inserting document with 3 pages

pages = 1
title = "web page 1"

pages = 3
title = "Lab1"

pages = 4
title = "history paper"

After inserting document with 1 page

pages = 1
title = "web page 1"

pages = 1
title = "receipt"

pages = 3
title = "Lab1"

pages = 4
title = "history paper"

The PriorityQueue Class

- Java provides a `PriorityQueue<E>` class that implements the `Queue<E>` interface
- `peek`, `poll`, and `remove` methods return the *smallest* item in the queue

Method	Behavior
<code>boolean offer(E item)</code>	Inserts an item into the queue. Returns true if successful; returns false if the item could not be inserted.
<code>E remove()</code>	Removes the smallest entry and returns it if the queue is not empty. If the queue is empty, throws a <code>NoSuchElementException</code> .
<code>E poll()</code>	Removes the smallest entry and returns it. If the queue is empty, returns null .
<code>E peek()</code>	Returns the smallest entry without removing it. If the queue is empty, returns null .
<code>E element()</code>	Returns the smallest entry without removing it. If the queue is empty, throws a <code>NoSuchElementException</code> .

Using a Heap to Implement a Priority Queue

- In a priority queue, just like a heap, the smallest item always is removed first
- Heap insertion and removal is $O(\log n)$
- The `java.util.PriorityQueue` uses an `Object[]` array

KWPriorityQueue Class

Data Field	Attribute
<code>ArrayList<E> theData</code>	An <code>ArrayList</code> to hold the data.
<code>Comparator<E> comparator</code>	An optional object that implements the <code>Comparator<E></code> interface by providing a <code>compare</code> method.
Method	Behavior
<code>KWPriorityQueue()</code>	Constructs a heap-based priority queue that uses the elements' natural ordering.
<code>KWPriorityQueue(Comparator<E> comp)</code>	Constructs a heap-based priority queue that uses the <code>compare</code> method of <code>Comparator comp</code> to determine the ordering of the elements.
<code>private int compare(E left, E right)</code>	Compares two objects and returns a negative number if object <code>left</code> is less than object <code>right</code> , zero if they are equal, and a positive number if object <code>left</code> is greater than object <code>right</code> .
<code>private void swap(int i, int j)</code>	Exchanges the object references in <code>theData</code> at indexes <code>i</code> and <code>j</code> .